

The elimination method solves systems of linear equations by adding or subtracting equations to cancel out one variable, reducing it to a single-variable equation. By manipulating equations via multiplication, you make coefficients of one variable opposite, allowing for easy elimination and substitution to find the remaining values.

Elimination Method

Q. $x - y - 7 = 0$, $x + y - 11 = 0$

Sol. $x - y = 7$ (i)

$x + y = 11$ (ii)

Adding (i) and (ii)

$x - y = 7$

$x + y = 11$

$2x = 18$

$x = 9$

Substituting $x = 9$ in (ii)

$9 + y = 11$

$y = 11 - 9$

$y = 2$

$x = 9$ and $y = 2$ is the solution of the given simultaneous equations

Ex 3.3

Elimination method

① (i) $x + y = 5 \rightarrow \textcircled{1} \times 3$
 Coeff equal $2x - 3y = 4 \rightarrow \textcircled{2} \times 1$

$3x + 3y = 15 \rightarrow \textcircled{3}$

$2x - 3y = 4 \rightarrow \textcircled{4}$

$5x = 19$

$5x = 19$

$x = \frac{19}{5} \rightarrow \text{sub in eq } \textcircled{1}$

* Substitution method :-

$x + y = 5 \rightarrow \textcircled{1}$

$2x - 3y = 4 \rightarrow \textcircled{2}$

$x + y = 5$

$x = 5 - y \rightarrow \textcircled{1}$

sub in eqn ②

$x + y = 5$

$\frac{19}{5} + y = 5$

$y = \frac{5 \times 5 - 19}{5}$

$y = \frac{25 - 19}{5}$

$\therefore y = \frac{6}{5}$

1 check
 $x + y = 5$

$\frac{19}{5} + \frac{6}{5} = \frac{25}{5}$

$= 5$

(LHS = RHS)

③

$2x - 3y = 4$

$2(5 - y) - 3y = 4$

$10 - 2y - 3y = 4$

$10 - 5y = 4$

$-5y = 4 - 10$

$y = \frac{-6}{-5}$

$y = \frac{6}{5}$ sub in eqn

④

$x + y = 5$

$x + \frac{6}{5} = 5$

$x = 5 - \frac{6}{5}$

$x = \frac{25 - 6}{5}$

$x = \frac{19}{5}$

Q. (ii) Solve the following pair of linear equations by the elimination method (and the substitution method)

(ii) $3x + 4y - 10 = 0$ and $2x - 2y - 2 = 0$

Elimination method

$3x + 4y = 10 \rightarrow \textcircled{1} \times 2$

$2x - 2y = 2 \rightarrow \textcircled{2} \times 4$

$6x + 8y = 20$

$3x + 4y = 10$

$3(2) + 4y = 10$

$4y = 10 - 6$

$4y = 4$

check: $2x - 2y = 2$
 $2(2) - 2(1) = 2$
 $4 - 2 = 2$

$$\begin{array}{r}
 6x + 8y = 20 \\
 8x - 8y = 8 \\
 \hline
 14x = 28 \\
 x = 2
 \end{array}$$

$x = 2$ Sub in eq ①

Graphical Method

(iv) $x + 2y = 6$; $2x + y = 6$

$x + 2y = 6 \rightarrow$ ①

$x + 2y = 6 \rightarrow$ ①

If $x = 0 \Rightarrow 0 + 2y = 6$

$2y = 6$
 $y = \frac{6}{2} = 3$

$x + 2y = 6$
 $2y = 6 - x$
 $y = \frac{6 - x}{2}$

x	0	4
$y = \frac{6-x}{2}$	3	1
x, y	(0, 3)	(4, 1)

$\rightarrow$ eqn ①

$$\begin{aligned}
 4y &= 10 - 6 \\
 4y &= 4 \\
 y &= \frac{4}{4} = 1
 \end{aligned}$$

$y = 1$

The solution is $x = 2, y = 1$

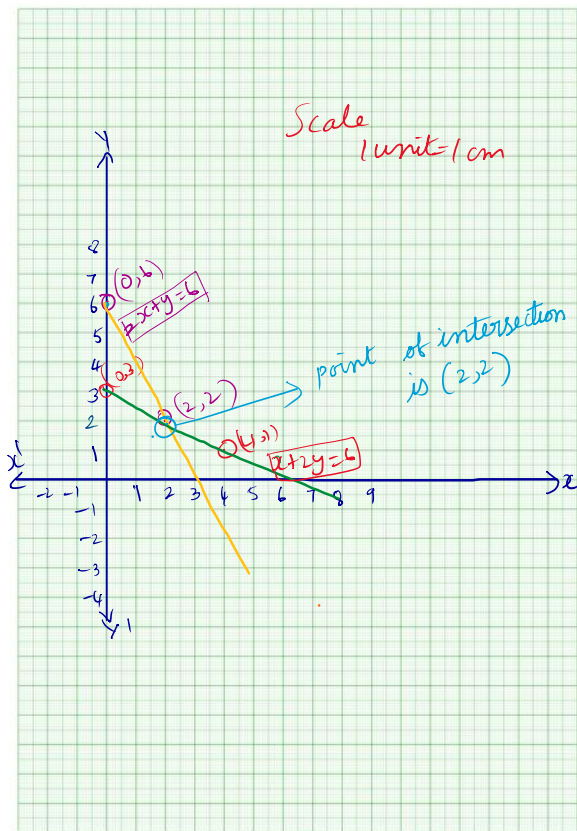
$2x + y = 6 \rightarrow$ ②

$y = 6 - 2x$

If $x = 0$
 $y = 6 - 2(0)$
 $y = 6$

If $x = 2$
 $y = 6 - 2(2)$
 $y = 6 - 4 = 2$

x	0	2
$y = 6 - 2x$	6	2
(x, y)	(0, 6)	(2, 2)



eqn ① intercept

$$x, y = A(0, 3) \quad B(4, 1)$$

eqn ② intercept

$$(x, y) = (0, 6) (2, 4)$$

∴ The point of intersection is $(2, 2)$