

- ① Determine whether $x = -\frac{1}{2}$, $x = \frac{1}{3}$ are the solutions of the given eqn $6x^2 - x - 2 = 0$ or not.

Ans $P(x) = 6x^2 - x - 2$

$$P(-\frac{1}{2}) = 6(-\frac{1}{2})^2 - (-\frac{1}{2}) - 2$$

$$= 6(\frac{1}{4}) + \frac{1}{2} - 2$$

$$= \frac{3}{2} + \frac{1}{2} - 2$$

$$= \frac{3+1-4}{2} = \frac{0}{2} = 0$$

$$\therefore P(-\frac{1}{2}) = 0$$

So $x = -\frac{1}{2}$ is a solution of given equation

Put $x = \frac{1}{3}$

$$P(x) = 6x^2 - x - 2$$

$$P(\frac{1}{3}) = 6(\frac{1}{3})^2 - \frac{1}{3} - 2$$

$$= \frac{6 \times 1}{3 \times 3} - \frac{1}{3} - 2$$

$$= \frac{2-1-6}{3}$$

$$= \frac{-5}{3} \neq 0$$

$$P(\frac{1}{3}) \neq 0$$

$\therefore x = \frac{1}{3}$ is not a solution of the given equation.

- ② In each of the following equations determine the value of k for which the given values is a solution of the equation.

(i) $kx^2 + 2x - 3 = 0$, $x = 2$

put $x = 2$ in eqn

$$k(2)^2 + 2(2) - 3 = 0$$

$$4k + 4 - 3 = 0$$

$$4k + 1 = 0$$

$$4k = -1$$

$$\therefore k = -\frac{1}{4}$$

(ii) $x^2 + 2ax - k = 0$, $x = -a$

$$(-a)^2 + 2a(-a) - k = 0$$

$$a^2 + (-2a^2) - k = 0$$

$$-a^2 - k = 0$$

$$-a^2 = k$$

$$\therefore k = -a^2$$

$$x^2 + 2ax - k = 0$$

$$(-a)^2 + 2a(-a) - k = 0$$

$$a^2 - 2a^2 - k = 0$$

$$-a^2 - k = 0$$

$$-a^2 = k$$

$$k = -a^2$$

- ③ If $x = 2$ and $x = 3$ are roots of the equation $3x^2 - 2ax + 2b = 0$ find the value of a and b

Given $3x^2 - 2ax + 2b = 0 \rightarrow ①$

put $x = 2$ and $x = 3$ in eqn ①

$$x = 2,$$

$$3(2)^2 - 2a(2) + 2b = 0$$

$$3(4) - 4a + 2b = 0$$

$$-4a + 2b = -12$$

$$4a - 2b = 12 \div 2$$

$$2a - b = 6 \rightarrow ②$$

$$x = 3,$$

$$3(3)^2 - 2a(3) + 2b = 0$$

$$27 - 6a + 2b = 0$$

$$\Rightarrow 6a - 2b = 27 \rightarrow ③$$

$$2a - b = 6 \times 2$$

$$6a - 2b = 27 \times 1$$

$$4a - 2b = 12$$

$$6a - 2b = 27$$

$$-2a = 15$$

$$2a = 15$$

$$a = \frac{15}{2}$$

sub in eq ②

$$x(\frac{15}{2}) - b = 6$$

$$-b = 6 - 15$$

$$b = 9$$

$\therefore$ Required values

$$a = \frac{15}{2}$$

$$b = 9$$

Q) Solve the following quadratic equations by factorization method

i) $3x^2 + 34x + 11 = 0$

Sol: $3x^2 + 34x + 11 = 0$

$$\therefore 3x^2 + x + 33x + 11 = 0$$

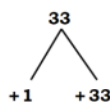
$$\therefore x(3x + 1) + 11(3x + 1) = 0$$

$$\therefore (3x + 1)(x + 11) = 0$$

$$\therefore 3x + 1 = 0 \text{ or } x + 11 = 0$$

$$\therefore 3x = -1 \text{ or } x = -11$$

$$\therefore x = -\frac{1}{3} \text{ or } x = -11$$



To factorise by splitting middle term

Find product of 3rd no. with 1st no.

Find two factors of 33 in such a way that by adding factors we get middle no.

Since, last sign is + Give middle sign to both factors.

The roots of the given quadratic equations are -11 and $-\frac{1}{3}$

Q) Solve the following quadratic equations by factorization method

iii) $2m^2 + 19m + 30 = 0$

$$\begin{cases} 2m^2 + 30 + 19m = 0 \\ 2m^2 = -19m - 30 \\ \text{Bring it to standard form} \end{cases}$$

$$2m^2 + 19m + 30 = 0$$

$$2m^2 + 15m + 4m + 30 = 0$$

$$m(2m+15) + 2(2m+15) = 0$$

$$(2m+15)(m+2) = 0$$

$$\Rightarrow 2m+15=0, m+2=0$$

$$2m = -15, m = -2$$

$$m = -\frac{15}{2}, m = -2$$

$\therefore$ The roots of given quadratic eqn are $-\frac{15}{2}$ and -2

$$(x+2)(x+3) = 3$$

$$x^2 + 3x + 2x + 6 = 3$$

$$x^2 + 5x + 3 = 0$$

$$2 \times 30 = 60$$

$$\begin{array}{r} 60 \quad 19 \\ 15 \quad 4 \end{array}$$

$$\begin{array}{r} 2 \overline{) 60} \\ 2 \overline{) 30} \\ 1 \overline{) 15} \end{array}$$

$$\begin{array}{r} 45 \times 4 = 60 \\ 15 + 4 = 19 \end{array}$$

Q) Solve the following quadratic equations by factorization method

iv) $x^2 - x - 132 = 0$

$$x^2 + 11x - 12x - 132 = 0$$

$$x^2 + 11x - 12x - 132 = 0$$

$$x(x+11) - 12(x+11) = 0$$

$$(x+11)(x-12) = 0$$

$$(x+11) = 0, (x-12) = 0$$

$$x = -11, x = 12$$

$$\begin{array}{r} 11 \quad 132 \\ 12 \end{array}$$

$$\begin{array}{r} -132 \\ -11 \quad +12 \end{array}$$

Solve the following by using formula method

i) $3q^2 = 2q + 8$

Sol: $3q^2 = 2q + 8$

$$\therefore 3q^2 - 2q - 8 = 0$$

On comparing with $ax^2 + bx + c = 0$, we get, $a = 3$, $b = -2$ & $c = -8$

$$b^2 - 4ac = (-2)^2 - 4(3)(-8)$$

$$= 4 + 96$$

$$= 100$$

$$D > 0$$

$$\therefore q = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\therefore q = \frac{-(-2) \pm \sqrt{100}}{2(3)}$$

$$\therefore q = \frac{2 \pm 10}{6}$$

$$q = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \Rightarrow q = \frac{-b \pm \sqrt{D}}{2a}$$

$$\therefore q = \frac{2+10}{6} \text{ or } q = \frac{2-10}{6}$$

$$\therefore q = \frac{12}{6} \text{ or } q = \frac{-8}{6}$$

$$\therefore q = 2 \text{ or } q = -\frac{4}{3}$$

The roots of the given quadratic equations are 2 and $-\frac{4}{3}$

$$D = -1 < 0$$

$$\begin{array}{l} D \geq 0 \\ D > 0 \\ D = 0 \end{array}$$

Relationship between discriminant and nature of the roots

When $D = 0 \Rightarrow b^2 - 4ac = 0 \Rightarrow$ Two equal real roots
 $D > 0 \Rightarrow b^2 - 4ac > 0 \Rightarrow$ Two distinct real roots
 $D < 0 \Rightarrow b^2 - 4ac < 0 \Rightarrow$ No real roots or 2 roots

Case ② $\Rightarrow$

Case ③ $\Rightarrow$

$$D < 0$$

$b^2 - 4ac < 0 \Rightarrow$ roots
No real roots or
imaginary roots.

Proof
Assume integers

$$\sqrt{n+1} + \sqrt{n-1} = x \quad (\text{where } x \text{ is rational})$$

squaring on both sides

$$(\sqrt{n+1} + \sqrt{n-1})^2 = x^2$$

$$(a+b)^2 = a^2 + b^2 + 2ab$$

$$(n+1) + (n-1) + 2\sqrt{(n+1)(n-1)} = x^2 \rightarrow (a+b)(a-b) = a^2 - b^2$$

$$2n + 2\sqrt{n^2-1} = x^2$$

$$2\sqrt{n^2-1} = x^2 - 2n$$

Since RHS is rational $\sqrt{n^2-1}$ must be rational

So $n^2-1 = k^2$ for some integer k .

$$n^2 - k^2 = 1 \Rightarrow (n-k)(n+k) = 1$$

$$n=1$$

But for $n=1$

$$\sqrt{n+1} + \sqrt{n-1} = \sqrt{1+1} + \sqrt{1-1}$$

$$= \sqrt{2} + 0$$

$= \sqrt{2}$ is irrational

This is contradiction.

$\therefore$ There is no positive integer n for which $\sqrt{n+1} + \sqrt{n-1}$ is rational

$$\begin{aligned} n-k &= 1 \\ n+k &= 1 \quad \text{add} \\ \hline 2n &= 2 \\ n &= 1 \end{aligned}$$